

Comments by Rafael Repullo on

**Monetary Easing, Investment and
Financial Instability**

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Purpose of paper

- Optimal monetary policy with financial stability concerns
- Specifically: Construct a model that explains three facts
 - Lax monetary policy
 - High payouts of firms to shareholders
 - Excessive risk-taking

Model overview (i)

- OLG model
 - 2-period lived workers and entrepreneurs
 - Monetary and fiscal authority
- Workers
 - Unit endowment of labor when young
 - Can supply labor to market or work in private production
 - Private production yields current output
 - Wages paid when young
 - Only interested in consumption when old

Model overview (ii)

- Entrepreneurs

- Demand labor to produce future output

- Utility depends on sum of current and future consumption

- Need to borrow to pay wages + current consumption

- Monetary authority

- Can set the real interest rate

- Can resort to fiscal authority to balance its books

Main results (i)

- Characterize steady state equilibrium
- Analyze effects of increase in market supply of labor
 - With flexible wages: Central bank does nothing
 - With fixed wages: Central bank reduces the real rate
 - Increases borrowing by entrepreneurs

Main results (ii)

- To address implications for financial stability
 - Modified model with 3-period lived entrepreneurs
 - Output produced at $t + 2$, but wages paid at t
 - Borrowing has to be rolled over at $t + 1$
 - Exogenous probability of not being able to borrow at $t + 1$
- A reduction in real rate by central bank
 - Increases borrowing by entrepreneurs
 - Increases rollover risk: Financial instability
 - But central bank can act as lender of last resort

Main comments (i)

- Model assumes that central bank can set the real interest rate
 - Assumption is becoming popular in recent literature
 - But is nevertheless quite restrictive
 - Link between nominal and real rates may not be trivial

Main comments (ii)

- Entrepreneurs' preferences produce jumps in consumption
 - Entrepreneurs' consumption decision problem

$$\max_{(c_0, c_1)} (c_0 + c_1) \quad \text{subject to} \quad c_0 + \frac{1}{r} c_1 = y$$

→ Solution

$$c_0(r) = \begin{cases} 0, & \text{if } r > 1 \\ y, & \text{if } r < 1 \end{cases}$$

- A reduction in r below 1 leads to jump in borrowing
 - Large effects of monetary policy on consumption
 - and on financial stability

Main comments (iii)

- Discussion on financial stability is pretty ad hoc
 - Based on exogenous probability of rollover
 - It would be desirable to have something more structural

What am I going to do?

- Present a slightly different version of the model
 - No OLG structure
 - No jumps in the consumption of entrepreneurs
 - Parametric specification of production and utility functions
- Focus on the working of monetary policy
 - Ignoring the discussion on financial stability

Part 1

Model with flexible wages

Model setup

- Two dates ($t = 0, 1$)
- Two consumption goods (at dates $t = 0, 1$) plus labor at $t = 0$
- Two types of private agents: workers and entrepreneurs
- Markets available at $t = 0$
 - Labor market with wage w (in terms of the good at $t = 0$)
 - Bond market with gross real rate r

Workers

- Continuum of workers characterized by
 - Unit labor endowment at $t = 0$
 - Fraction l supplied to market at wage w
 - Fraction $1 - l$ invested in private production
 - Production function $g(1 - l)$ of good at $t = 0$
 - Only interested in consumption at $t = 1$

$$c_w = r \max_l [wl + g(1 - l)]$$

Entrepreneurs

- Continuum of entrepreneurs characterized by
 - Production function $f(l)$ of good at $t = 1$
 - Utility function

$$u(c_0, c_1) = \ln c_0 + \ln c_1$$

- Labor demand and consumption decisions

$$\max_{(l, c_0, c_1)} [\ln c_0 + \ln c_1]$$

subject to $c_0 + wl = \frac{1}{r}[f(l) - c_1]$

Parametric assumptions

- Workers' production function

$$g(1-l) = \rho\sqrt{1-l}$$

→ where ρ is productivity parameter used to shock the model

- Entrepreneurs' production function

$$f(l) = 2\sqrt{l}$$

Workers' decision rules

- Labor supply function

$$l(w) = \arg \max_l [wl + g(1-l)] = 1 - \frac{\rho^2}{4w^2}$$

→ Increasing in wage w

- Savings function

$$s(w) = \max_l [wl + g(1-l)] = w + \frac{\rho^2}{4w}$$

→ Increasing in wage w (for $l(w) > 0$)

Entrepreneurs' decision rules (i)

- Labor demand function

$$l(w, r) = \arg \max_l \left[\frac{1}{r} f(l) - wl \right] = \frac{1}{(wr)^2}$$

→ Decreasing in wage w

→ Decreasing in real rate r

- Current consumption function

$$c_0(w, r) = \frac{1}{2} \left[\frac{1}{r} f(l) - wl \right] = \frac{1}{2wr^2}$$

→ Decreasing in wage w

→ Decreasing in real rate r

Entrepreneurs' decision rules (ii)

- Borrowing function

$$b(w, r) = c_0(w, r) + wl(w, r) = \frac{3}{2wr^2}$$

→ Decreasing in wage w

→ Decreasing in real rate r

Equilibrium conditions

- Labor market

$$l(w) = l(w, r)$$

- Bond market

$$s(w) = wl(w) + g(1 - l(w)) = wl(w, r) + c_0(w, r) = b(w, r)$$

→ Using labor market equilibrium, this simplifies to

$$\underbrace{g(1 - l(w))}_{\substack{\text{Workers' output} \\ \text{at } t=0}} = \underbrace{c_0(w, r)}_{\substack{\text{Entrepreneurs'} \\ \text{consumption at } t=0}}$$

Equilibrium prices and quantities

- Wage: $w^* = \sqrt{5}\rho / 2$
- Real rate: $r^* = 1 / \rho$
- Labor supplied to market: $l^* = 4 / 5$
- Workers' consumption (and utility): $c_w^* = u_w^* = 3 / \sqrt{5}$
- Entrepreneurs' consumption at $t = 0$: $c_0^* = \rho / \sqrt{5}$
- Entrepreneurs' consumption at $t = 1$: $c_1^* = 1 / \sqrt{5}$
- Entrepreneurs' utility: $u_e^* = \ln \rho - \ln 5$

Shock to the workers' production function

- Consider a negative shock to workers' production function
→ Going from $\rho = 1$ to $\rho = 1/2$
- Comparison between the two equilibria

	w^*	r^*	l^*	u_w^*	c_0^*	c_1^*	u_e^*
$\rho = 1$	1.12	1	0.8	1.34	0.45	0.45	-1.61
$\rho = 1/2$	0.56	2	0.8	1.34	0.22	0.45	-2.30

Part 2

Model with fixed (real) wages

Fixed wages (i)

- Suppose that following the reduction in ρ wages do not fall
 - Excess supply of labor
 - No change in decision rules of entrepreneurs
 - Employment determined by labor demand $l(w^*, r)$

Fixed wages (ii)

- What will happen to the real rate?

→ Workers' output

$$\rho\sqrt{1-l(w^*, r)}$$

→ Equilibrium condition

$$\rho\sqrt{1-l(w^*, r)} = c_0(w^*, r)$$

→ For $\rho = 1/2$ we have $r = 1.17$

Equilibrium with fixed wages

- Comparison between the three equilibria

→ Third row corresponds to equilibrium with fixed wages

	w^*	r^*	l^*	u_w^*	c_0^*	c_1^*	u_e^*
$\rho = 1$	1.12	1	0.8	1.34	0.45	0.45	-1.61
$\rho = 1/2$	0.56	2	0.8	1.34	0.22	0.45	-2.30
$\rho = 1/2$	1.12	1.17	0.58	1.14	0.32	0.38	-2.11

Monetary easing (i)

- Suppose now that central bank reduces real rate to $r = 1$
→ Fourth row corresponds to new equilibrium

	w^*	r^*	l^*	u_w^*	c_0^*	c_1^*	u_e^*
$\rho = 1$	1.12	1	0.8	1.34	0.45	0.45	-1.61
$\rho = 1/2$	0.56	2	0.8	1.34	0.22	0.45	-2.30
$\rho = 1/2$	1.12	1.17	0.58	1.14	0.32	0.38	-2.11
$\rho = 1/2$	1.12	1	0.8	1.12	0.45	0.45	-1.61

Summing up

- Monetary easing when wages are rigid downwards leads to
 - Increase in labor supplied to the market
 - Reduction in workers' consumption and utility
 - Increase in entrepreneur's consumption and utility
 - Hence, not Pareto improving

Part 3
Discussion

Discussion

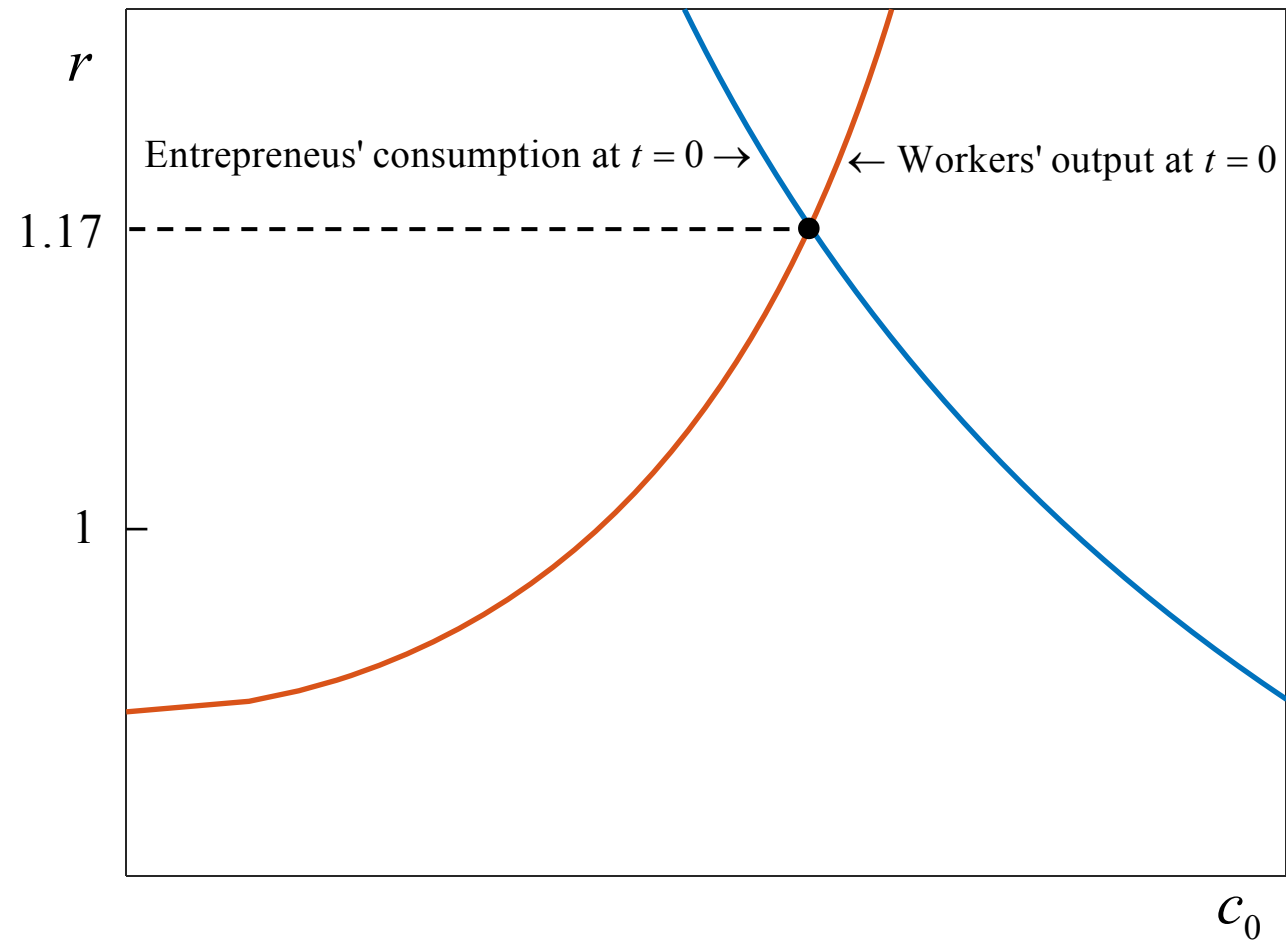
- Two questions
 - How can the central bank reduce the real rate?
 - What are the implications for the real economy

How can central bank reduce the real rate?

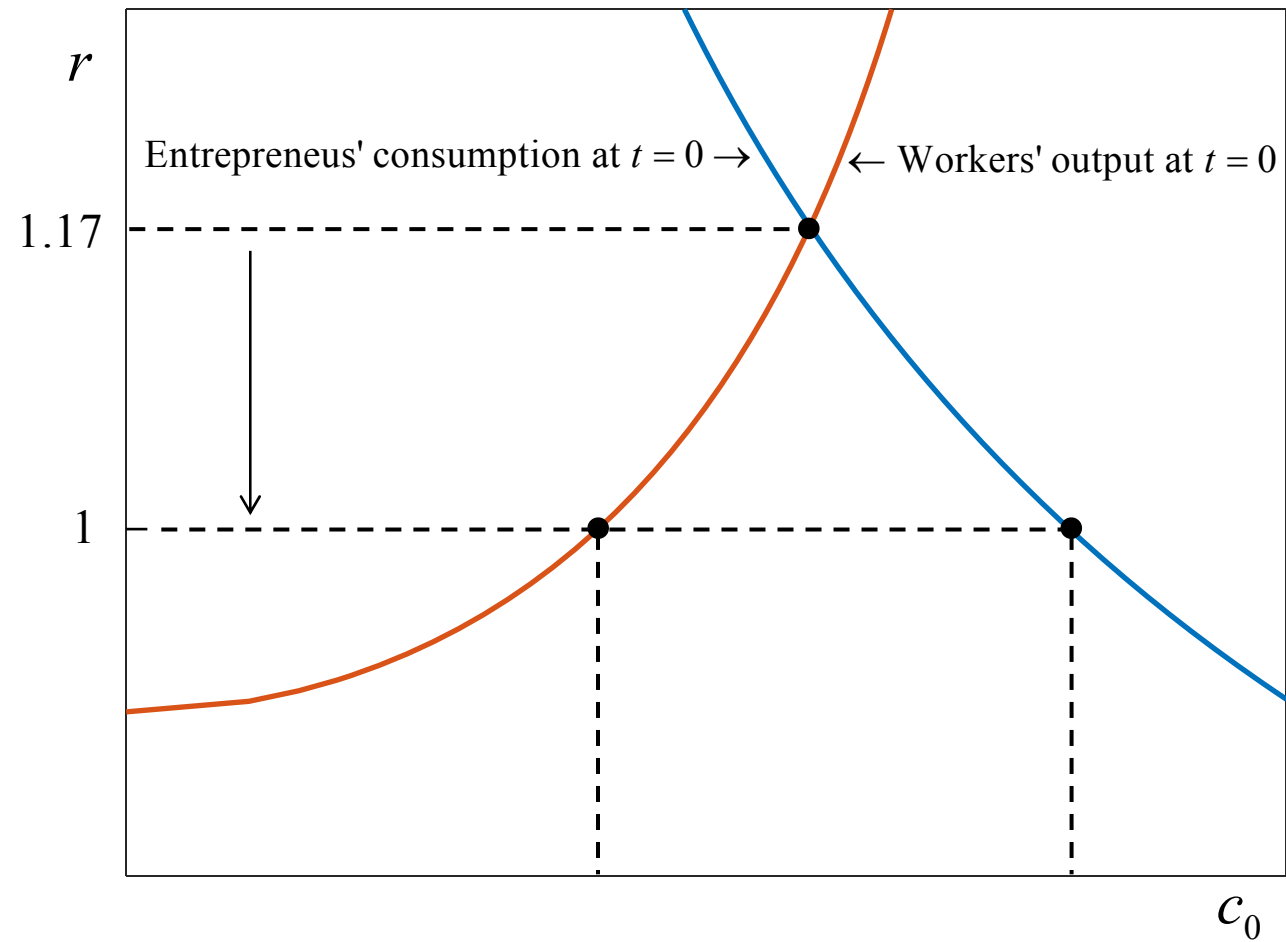
- In the equilibrium with fixed wages the real rate is $r = 1.17$
 - To reduce the real rate to $r = 1$ bond market has to clear
 - But for $r = 1$ there is an excess demand for savings
 - Central bank has to act as a supplier of savings
- Recall that bond market equilibrium simplifies to

$$\underbrace{g(1 - l(w^*, r))}_{\text{Workers' output at } t=0} = \underbrace{c_0(w^*, r)}_{\text{Entrepreneurs' consumption at } t=0}$$

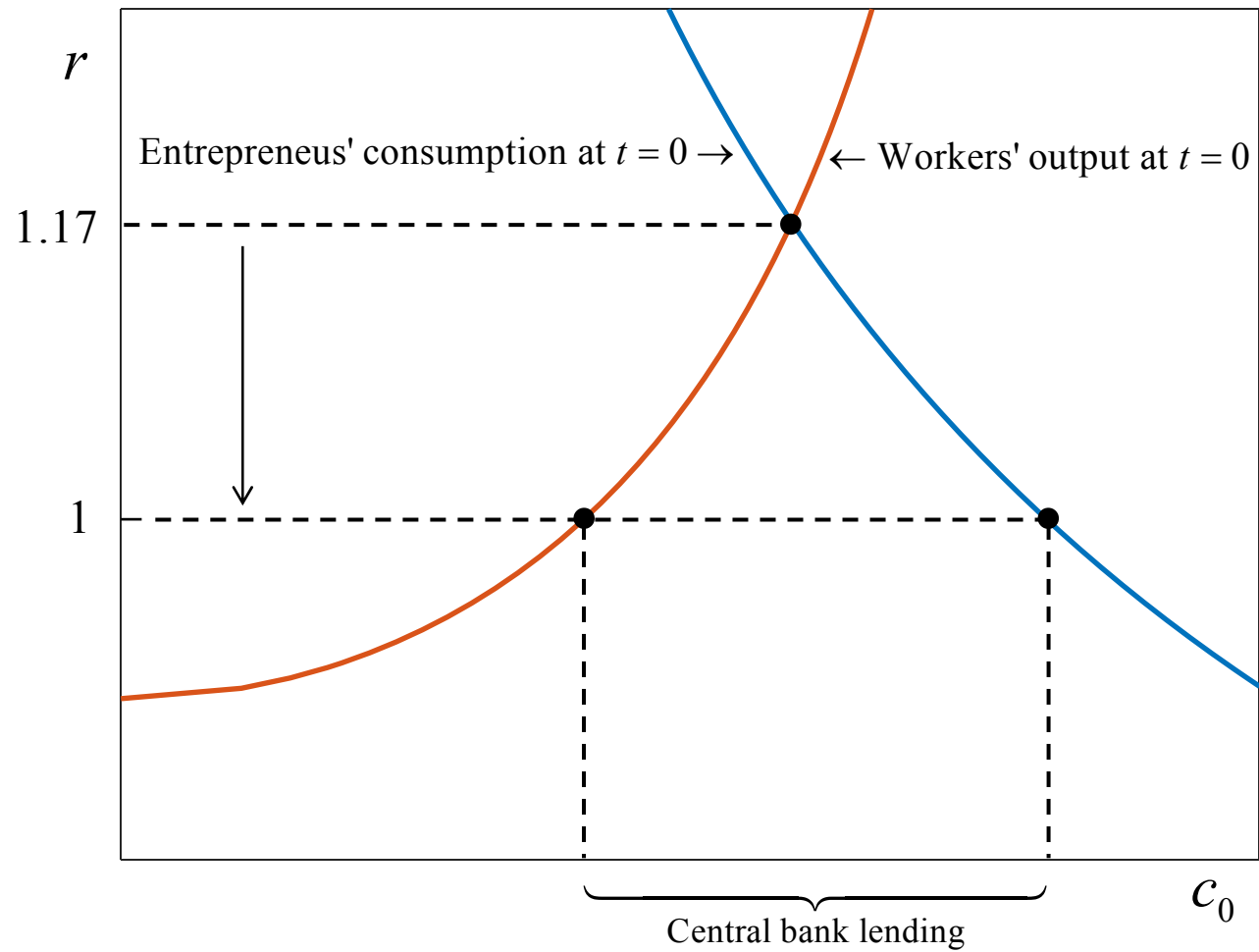
Bond market equilibrium under fixed wages



Bond market equilibrium under fixed wages



Bond market equilibrium under fixed wages



Implementing monetary easing (i)

- To implement the reduction in the real rate
 - Central bank has to be able to lend to the entrepreneurs
- Central bank is effectively a warehouse
 - that stores the consumption good
 - and lends it to the entrepreneurs

Implementing monetary easing (ii)

- Where do the goods in warehouse come from?
 - Taxing an initial generation of workers
- Central bank may get profits or losses (zero when $r = 1$)
 - Transferred to workers or entrepreneurs
- Connection between monetary and fiscal authorities

Implications for the real economy

- Construct the utility possibility frontier

$$\max c_w$$

$$\text{subject to: } c_w + c_1 = f(l)$$

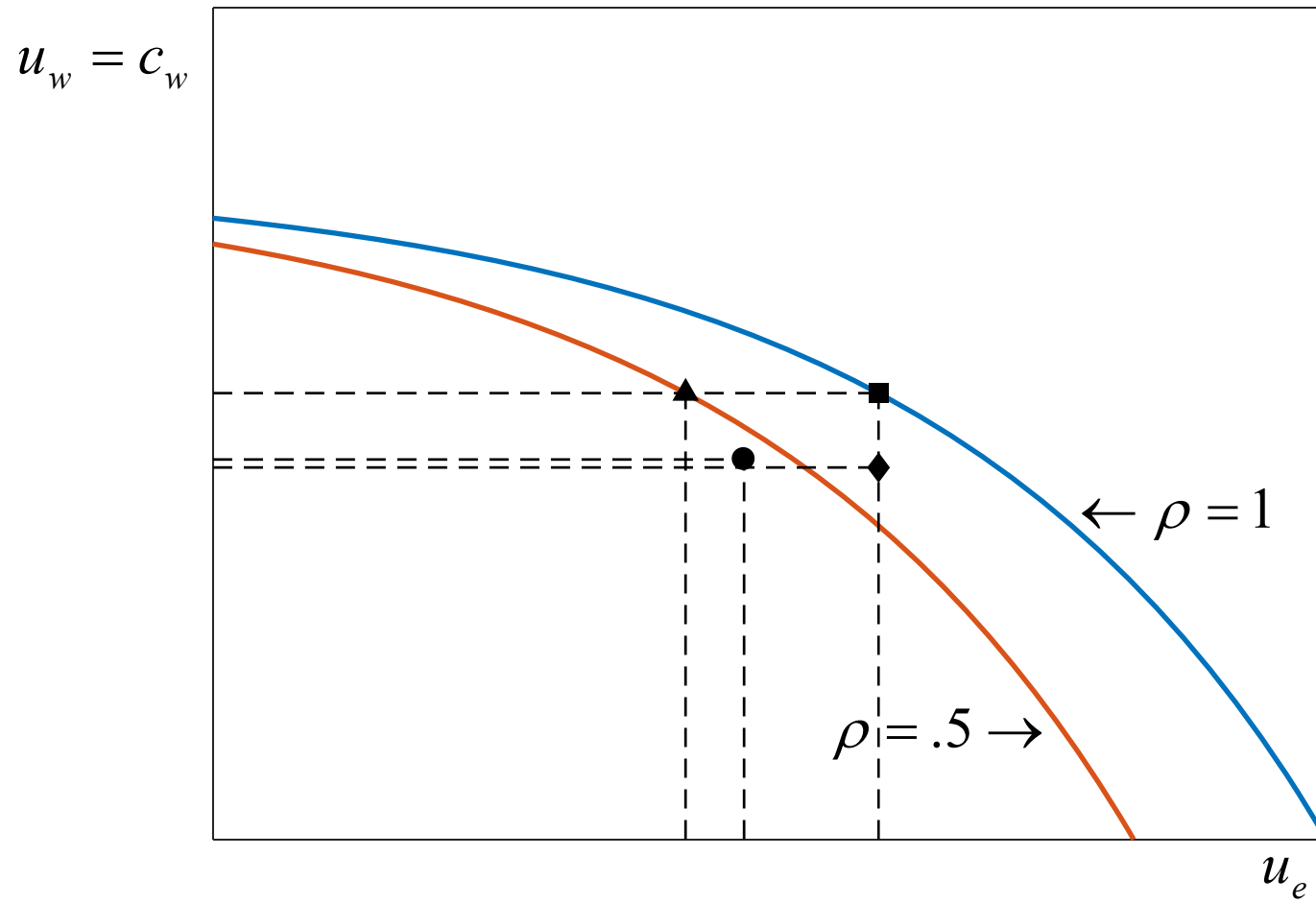
$$c_0 = g(1-l)$$

$$\ln c_0 + \ln c_1 = u_e$$

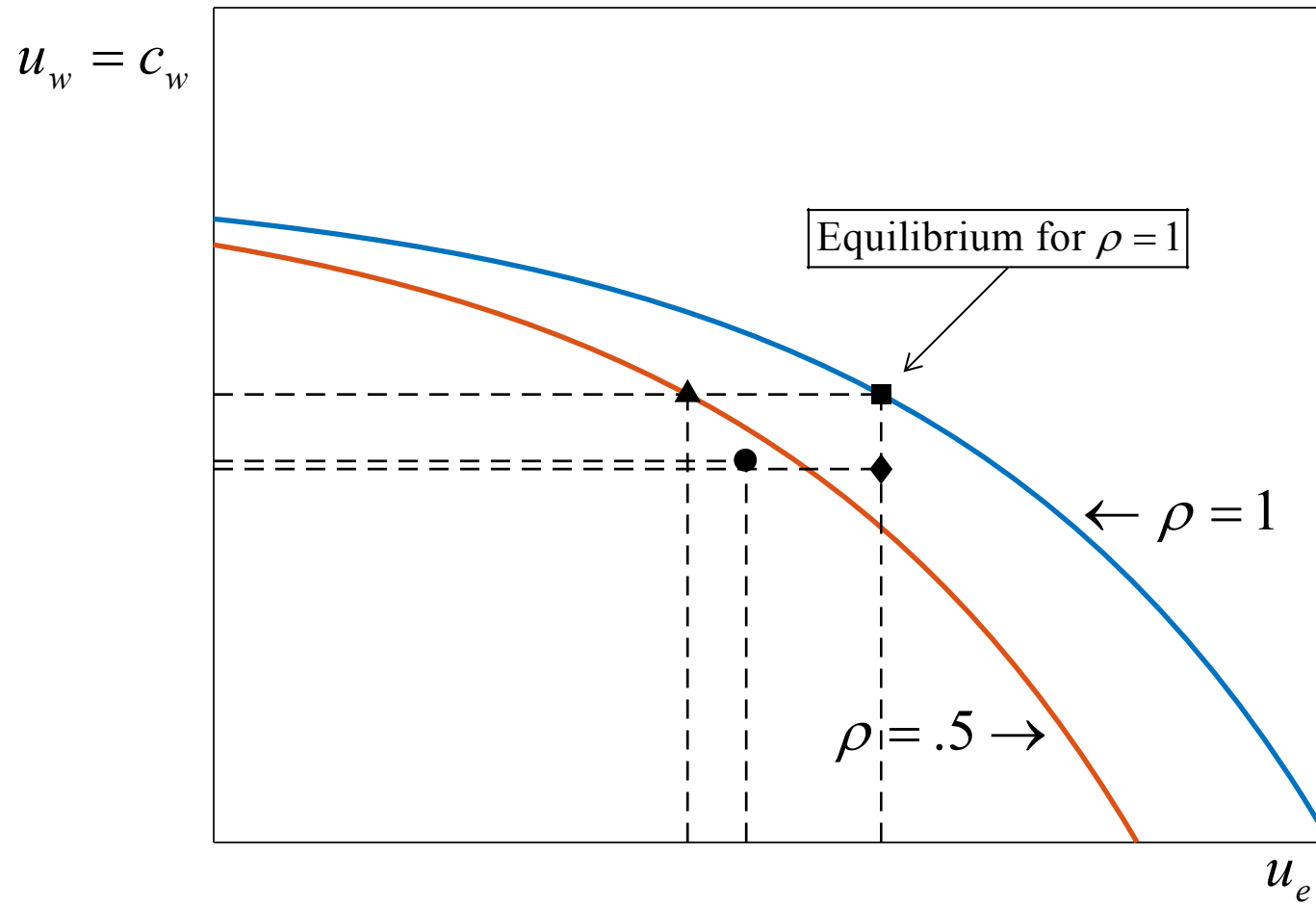
- Plot frontiers for from $\rho = 1$ to $\rho = 1/2$

→ Locate the different equilibrium points in utility space

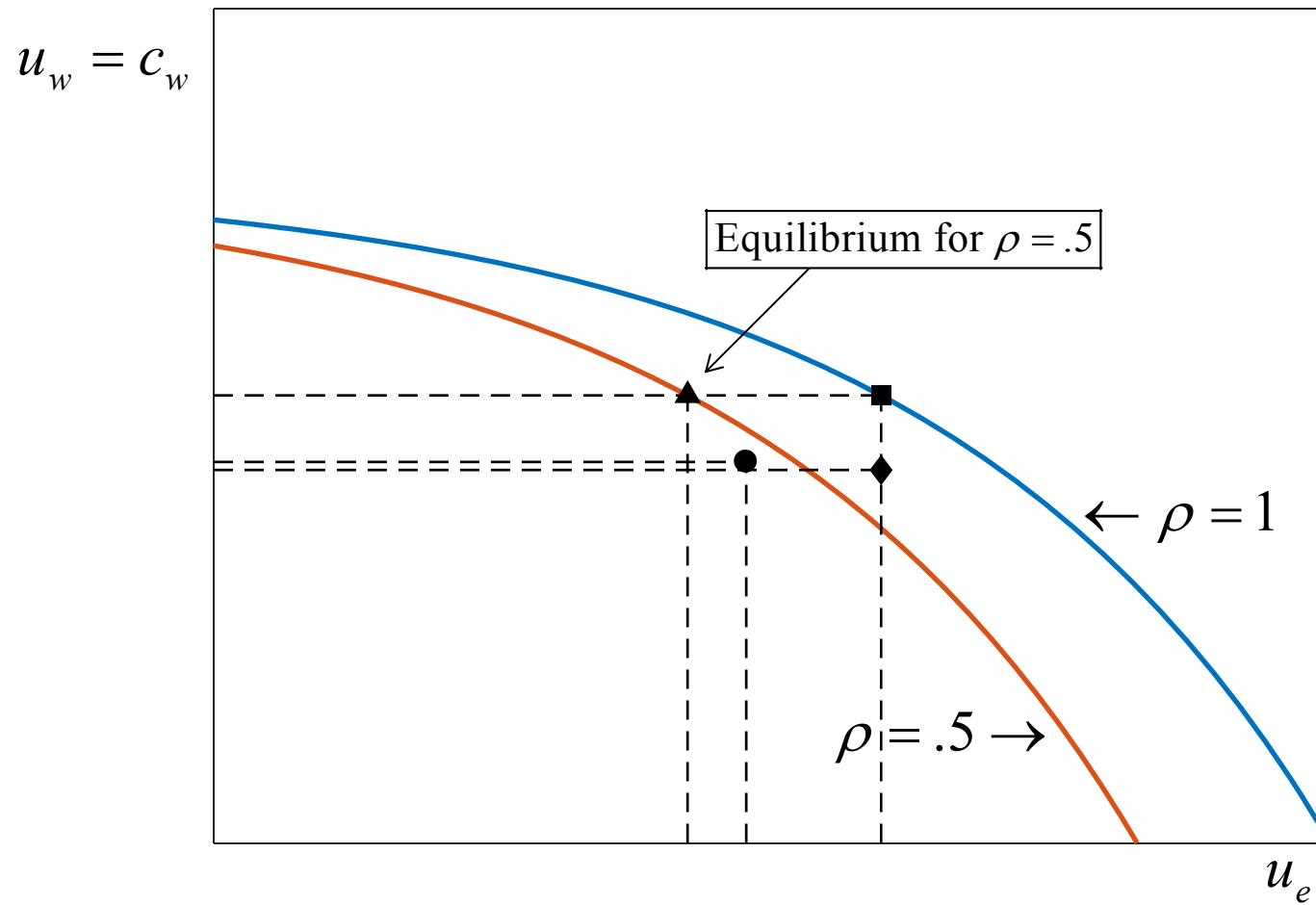
Utility possibility frontier



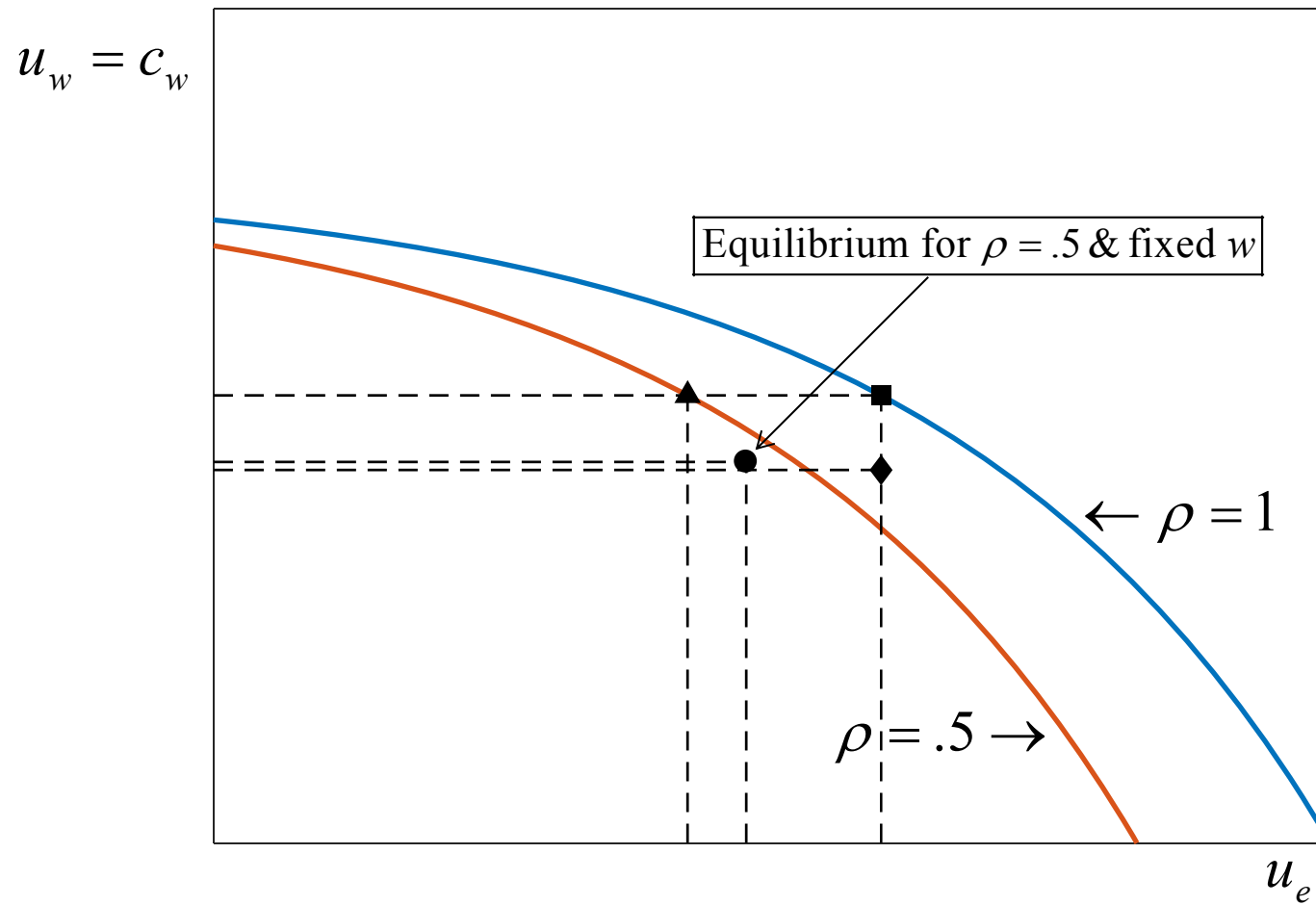
Utility possibility frontier



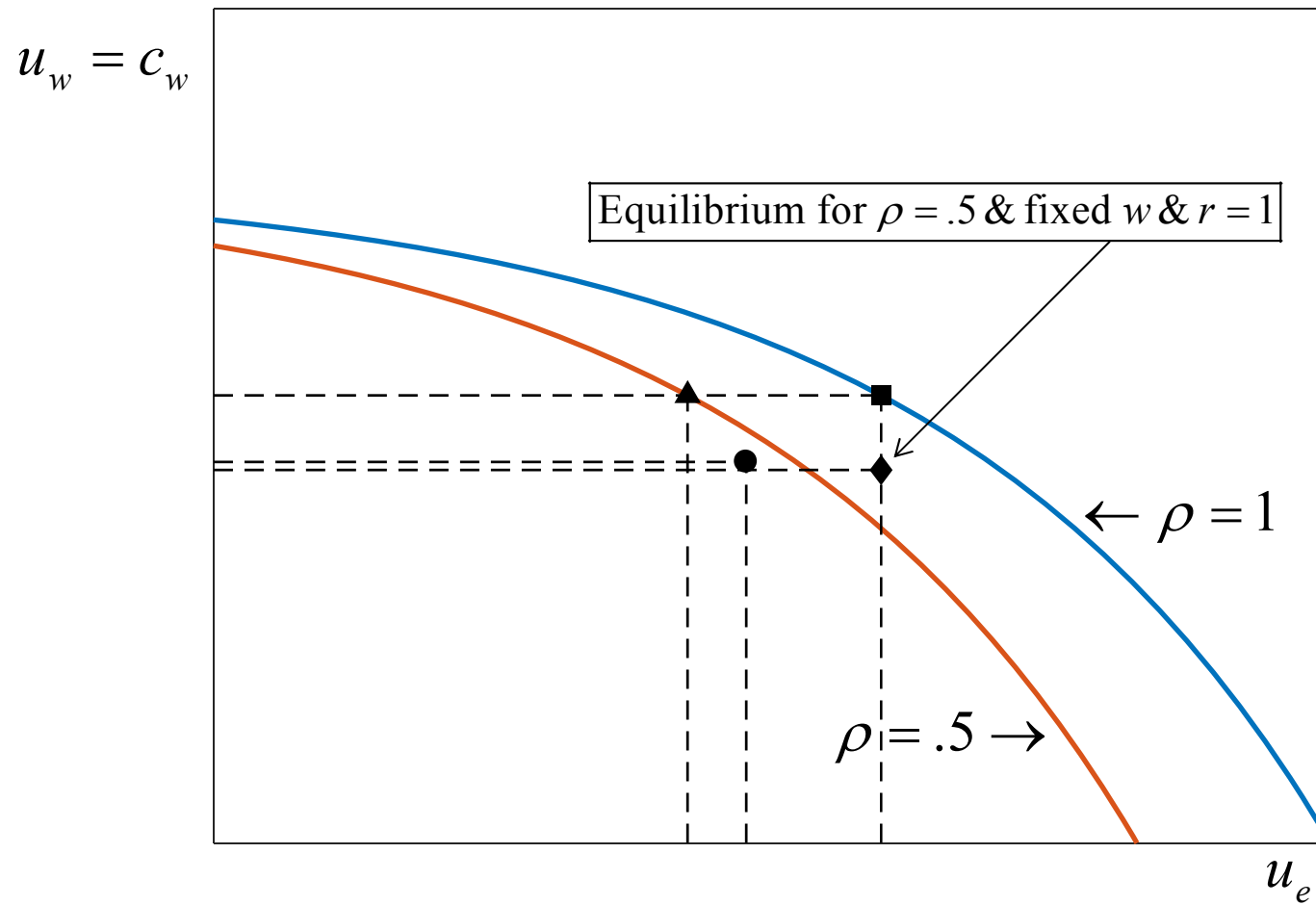
Utility possibility frontier



Utility possibility frontier



Utility possibility frontier



Summing up

- Equilibria with flexible wages are located on the frontiers
- Equilibrium with fixed wages is Pareto inefficient
- Equilibrium with monetary easing is outside the frontier
 - Central bank brings something that was not before
- Equilibrium with monetary easing is not Pareto improving
 - Distributional effects of monetary policy